Article

An Economic Analysis Algorithm for Urban Forestry Projects

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Received: 9 November 2018; Accepted: 31 December 2018; Published: 9 January 2019

Abstract: The second half of the 20th century was characterized by rapid growth of the urban population and lack of attention to environmental quality in the urbanizes territories. Thus, the development of many cities during that period took place through policies which, over time, resulted in a disaggregated landscape, both in morphological and functional terms. In some cases, these policies have caused the creation of land portions without a specific characterization, and the generation of urban voids that negatively affect the city’s development. To solve this problem, the public administration sectors of many countries are looking for new intervention strategies that are feasible from a social and economic point of view which are able to guarantee sustainable development. From this perspective, the execution of urban regeneration initiatives, including forestation, allows for the improvement of both environmental quality and citizens’ well-being, and promotes economic development. Considering the multiple effects that these initiatives can generate and the limited availability of public and private resources, it is appropriate to use multi-criteria decision support tools through which it is possible to evaluate the interventions’ complexity and best identify the city areas that lend themselves to be recovered and improved through the forestation. The aim of this work is to develop a support tool for public administrations aimed at identifying the optimal forestry projects’ location according to criteria that not only refer to financial type, but also their social, cultural, and environmental nature. Using Discrete Linear Programming algorithms, the model has been tested through a theoretical case study and reveals the advantages and limitations of the model, as well as future research prospects.

Keywords: sustainable development; urban renewal; urban forestry; ecosystem services; multicriteria analysis; Discrete Linear Programming

1. Introduction

Since the second half of the 20th century, the urban landscape of many cities has developed into a polycentric configuration in which there are often both areas with excessive building density, strong pollution, and high social disadvantage, as well as abandoned ones and others not only urbanized [1–4]. This situation has almost always caused a great difference between dissimilar parts of the same city, in terms of liveability, wealth, social equity, and environmental quality.

However, the presence in urban, often central contexts of free or partially built-up areas—hereon referred to as “degraded areas”—offers today the opportunity to reconnect the existing fabric on the
basis of territory unitary development models that can be traced back to the Green City integrated principles [5–7].

In 2015, the United Nations (UN) Organization approved the Global Sustainable Development Agenda, where the 17 Sustainable Development Goals (SDGs) that Member States agreed to pursue by 2030 are defined [8]. Among these SDGs, one of which specifically has regard to sustainable cities, it is possible to identify some logical-functional relationships useful for determining optimal intervention policies from an integrated sustainable development perspective (Figure 1).
design phase of urban forestry interventions, as principles defined in terms of the place characteristics and objectives pursued [20]. Each of the key issues can be matched with a performance indicator, established on the basis of the status quo of the area in which the renewal projects, including urban forestry, can be implemented, following SDGs and the ecosystemic effects generated in the reference urban context, hereinafter “Ecosystemic Integrated Projects” (EIPs).

The decision to realize EIPs in “degraded areas” was based on three targets, which concerned the possibility of providing a recreational space for the residents (recreational targets) with respect to the area’s morphological characteristics (structure-strengthening targets) and typological peculiarities of existing tree species (ecological targets) [16]. In this way, it is possible to recover “degraded areas” considering both the FAO’s key issues and targets according to a logical-functional relationship of biunivocal correspondence (see Figure 2 of Section 3.1). This also enables us to identify those that represent a possible city development node among the possible areas to be redeveloped, according to urban forestry-integrated principles [21].

Therefore, the problem arises of the best location choice for the urban renewal project, based on financial, social, cultural, and environmental criteria [6]. These are decisional problems of which resolution requires the use of specific economic evaluation techniques. In the case of jointly taking into account various kinds of indicators, it is useful to apply multi-criteria economic evaluation techniques in order to express the multidimensional character of the examined problem [22–24].

Operationally, different tools are known in the literature that can implement economic evaluation models based on multi-criteria logic, often constructed to solve ranking and sorting problems, as well as through optimization procedures [25,26]. Depending on the evaluation question to be solved and the consequent indicators to be adopted, it is possible to select the most appropriate evaluation tool [27]. Among these, the Operations Research Algorithms, such as Goal Programming [26], can certainly be extremely useful, since they allow for solving complex decision-making schemes with a high number of variables and multiple objectives to be pursued simultaneously [26]—as in the case of Ecosystemic Integrated Projects (EIPs)—through the writing of linear algebraic relationships between parameters, while respecting the specific multiple constraints of the problem to be solved [28].

Although the multiple positive repercussions generated by actions based on ecosystemic logics are now recognized, this intervention modality is still not widely used in urban policies. This is both due to the interest of the public administration and private sectors, which prefer actions that generate an immediate consensus return and financial repercussions, and the difficulty of realizing EIPs on the basis of evaluations that consider the multidimensional aspects and the use of multi-criteria proper of this type of project in an integrated manner [29].

2. Work Aims

In line with the framework outlined previously, our research objectives were first concerned with the need to focus on the investors and public administrators’ attention on the benefits of urban forestation projects for the redevelopment of degraded areas. Another more strictly operative objective consisted in defining an economic model which was able to select the areas to forest in an optimal manner, even in the presence of different kinds of constraints (technical, political, normative) and various stakeholders expressing conflicting interests and purposes. Thus, the sites, whose requalification made according to ecosystemic principles ensures the best result due to the availability of financial resources, the morphological characteristics, and the effect generated in the reference territorial context—assessed in terms of services offered to the community—were able to be identified.

In essence, starting from the set of available areas, financial resources, and effects that can be generated with forest interventions, we intended to define a decision support model for public administration technicians with which it was possible to:

- Generate a priorities list of the areas on which to implement the initiative due to the expected effects;
- generate favorite rational and awareness assessments;
• improve the transparency of the choices, translating the constraints and programme objectives into mathematic relations.

The novelty of this study should also be noted. Research on this topic in the literature is not very numerous and is actually rather recent. Studies which do exist represent an initial approach to the subject, which is addressed only in quite general terms [30].

Regarding the model to be defined and which was tested in this piece of research, it should be noted that according to the intervention methods and available data, it is possible to use different tools that are able to take into account the multidimensional character of the initiatives relating to the requalification of portions-circumscribed territories conducted in line with the EIP model. In this work, the theory and algorithms of Operational Research, with which it is possible to solve complex decision problems, and characterized by numerous constraints and many variables, were used. In particular this model was developed by crossing the linear programming algorithms with multi-criteria decision analysis (MCDA), and implemented using the “A Mathematical Programming Language” (AMPL) software. It is a simple and intuitive tool used for structuring mathematical programming problems. Resolutions can be made with the use of specific softwares for optimization models (solvers). Some examples of these are CPLEX, FortMP, and KNITRO [31,32].

The model was tested by using a case study. The model’s structure provides a general methodology that can be applied in complex planning cases. The model algorithm is easily adaptable to the specificity of various countries. This, through the writing of constraint relations, was defined according to the urban context of reference.

The remaining part of this paper is divided into four sections. In Section 3, the set of criteria that is defined and used for evaluating the intervention possibilities according to the objectives to be pursued and corresponding targets is outlined (Section 3.1), and a short background about Linear Programming principles is also provided, whereafter the decision support model is structured to optimize the financial resources allocation for EIPs that includes the forestation of urban fabric degraded areas (Section 3.2); in Section 4, the case study is illustrated and the model proposed is implemented, whereafter the results are explained; and in Section 5 the conclusions are reached.

3. Materials and Methods

3.1. Set of Criteria for the Selection of Sites to Be Renewed with Urban Forestry Interventions

In the case where there are degraded land portions which are poorly constructed or without a specific functional characterization, it may be useful to facilitate the execution of redevelopment interventions in the urban forestry ecosystemic principles. The general target benchmarks are the: psycho-physical wellbeing of citizens (recreational targets), existing natural component enhancement (ecological targets), and safeguarding of environmental, social, and cultural components of the area of interest (structure-strengthening targets) [6].

These targets are reflected in 14 evaluation criteria, identified by Van Elegem et al. (2002) (Figure 2c). These criteria can be used to formulate a complex judgment regarding the selection of territorial contexts that are best suited to being realigned. In fact, as illustrated in Figure 2, the 14 criteria allow for expression of the ability of the area to satisfy the key issues (Figure 2a) and pursue the targets through the use of appropriate indicators (Figure 2d).

In the literature, it appears that there are many indicators that express the criteria. In the case of forestry, these are indicators that are able to characterize the reference urban context to which the intervention reverts [17], and to express ecosystemic services of ecological-environmental [33–35], economic, social, and cultural [36] type.

Some indicators (e.g., number of inhabitants, accessibility, absence of heavy industry and road infrastructure, absence of recreation facilities, texture classes, presence of forests) are objective, and can be recognized and measured on the basis of detailed information regarding the reference urban context; on the other hand, the remaining indicators can be measured using an ordinal values scale, by
assigning to each of them a score according to the capacity of an EIP that includes urban forestry, to generate economic-environmental repercussions in the territory.

Figure 2. Logical sequence for the selection of evaluation indicators.

The logical scheme of Figure 2 allows to structure a multi-criteria evaluation model that can be used to facilitate the EIP execution in degraded areas, through the following phases:

1. Identification of the specific social, cultural, environmental, and financial objectives to be pursued;
2. selection of criteria and related performance indicators to express the achievement degree of the specific objectives set;
3. choice of the indicators selected on the basis of qualitative/quantitative information related to the reference urban context to the type of intervention proposed;
4. definition of the parameters and numerical data characteristics of the mathematical model related to the selection problem to be solved;
5. characterization of the mathematical model according to the logical-syntactic paradigms of mathematical programming software.

3.2. The Optimization Algorithm

For the definition of a model aimed at identifying the best urban area among those available to be used for redevelopment projects carried out according to ecosystemic principles of urban forestry, the Operational Research provides several algorithms, among which those of Linear Programming are most widely used.

In fact, complex problems, characterized by a high number of variables and constraint relations [37], as in the case of EIPs, are often solved using mathematical models structured according to goal programming. This is a methodology that helps to find an optimal solution by respecting the system constraints that characterize the problem to be solved. Starting from the second half of the last century, linear programming has been applied in numerous problems of project management [31,38–44] and land-use planning [45,46], as well as implementing geographic information systems [47–49], decision maps [50,51], urban-planning and economic project evaluation [52–55].
In particular, with reference to planning and urban regeneration, goal programming models are often used for the selection of the best project alternative between urban redevelopment interventions able to maximize the social welfare function [56–58], also referring to areas within strongly consolidated fabrics [59].

Again, some authors have used goal programming to develop a multi-criteria model to support revitalization strategies of the historic Alishan Forest Railway in Taiwan [60], or to characterize a model for urban regeneration interventions [61].

The development of an investment project has a number of similarities with the problem of Operational Research, which concerns the optimal allocation of scarce resources that can have alternative uses. In mathematical form, considering \( m \) available resources which may have \( n \) possible uses, the generic problem of operational research [62] is made of:

\[
\text{max} \ (\text{o min}) \ f(x_1, x_2, \ldots, x_n) \tag{1}
\]

with the constraints (2):

\[
\begin{align*}
\sum a_{ij} \times x_i & \leq b_i \\
\sum a_{ij} \times x_i & \leq b_i \\
\cdot & \\
\sum a_{ij} \times x_i & \leq b_i
\end{align*}
\tag{2}
\]

In Equations (1) and (2):

- \( f(x_1, x_2, \ldots, x_n) \) is the objective function to be maximized (max) or minimized (min);
- \( x_1, x_2, \ldots, x_n \) are the problem variables, on which the possible use of the resources depends;
- \( \sum a_{ij} \times x_i \leq b_i \) \((i = 1, \ldots, m \text{ and } j = 1, \ldots, n) \) defines the \( i \)-th constraint, where \( a_{ij} \) is the rate of the \( i \)-th resource in the \( j \)-th use and \( b_i \) is the \( i \)-th resource amount.

The functional relationships expressed in linear programming terms can be used to solve selection cases between design alternatives aimed at urban territory redevelopment [55,63–65], also with the implementation of Geographic Information Systems [47–49].

In these cases, these are often mathematical models characterized by the integer constraint \([x \in \{0,1\}]\) placed on the decision variables and resolved through the resolutive algorithms of Discrete Linear Programming (DLP). Among the most commonly used algorithms are those of dynamic programming, implicit enumeration (such as Branch & Bound), cutting plane algorithms, and the Branch & Cut algorithm [66,67].

In the present study, since each design alternative (intervention area) should be considered as unitary, given the objective of establishing whether to use or exclude it, it was possible to use Discrete Linear Programming (DLP) algorithms [68].

The “A Mathematical Programming Language” (AMPL) software was used to structure the model. In practice, the use of the AMPL programming environment allows to write the selection problem through the following steps:

1. Identification of the problem elements (specific objectives in relation to targets, number of areas, evaluation criteria) as a set of objects;
2. specification of the problem parameters (budget, costs, multi-criteria evaluation matrix) to be included in the system;
3. definition of the variables’ value (var \( x \) binary);
4. structuring of the objective function as a linear algebraic expression that maximizes the ability to pursue the multiple purposes of urban forestry initiatives;
5. specification of the problem constraints to be solved.
These steps define the structure of a model in parametric form (.mod file) to which the problem data are associated with a separately written .dat file.

On the basis of \( m \) targets for projects based on ecosystemic principles, the problem arises of selecting, among the \( n \) areas to be redeveloped, those most suitable to be transformed through urban forestry.

Each area, taken as the \( x_i \) variable of the problem, was evaluated on the basis of \( k \) evaluation criteria (C) defined according to the target \( m \)-th to be reached. Considering both the project investment cost \( C_i \) for the \( i \)-th area and the available budget, the linear relations of the following mathematical system (3) are:

\[
\begin{align*}
\max \sum (C_{1.1} + \cdots + C_{2.1} + C_{m.1}) x_i \\
\sum C_i x_i & \leq \text{BUDGET} \\
x & \in \{0, 1\} \quad (i = 1, \ldots, n)
\end{align*}
\]

These mathematical relationships were implemented in the AMPL programming environment, as shown in Table 1 [69].

Table 1. The evaluation model written in “A Mathematical Programming Language” (AMPL) software (.mod file).

<table>
<thead>
<tr>
<th>AREA SELECTION PROBLEM</th>
</tr>
</thead>
<tbody>
<tr>
<td>SETS</td>
</tr>
<tr>
<td>set AREAS;</td>
</tr>
<tr>
<td>set EVALUATION CRITERIA;</td>
</tr>
<tr>
<td>PARAMETERS</td>
</tr>
<tr>
<td>param BUDGET;</td>
</tr>
<tr>
<td>param MULTI-CRITERIA EVALUATION MATRIX {AREAS, EVALUATION CRITERIA};</td>
</tr>
<tr>
<td>param COST {AREAS};</td>
</tr>
<tr>
<td>VARIABLES</td>
</tr>
<tr>
<td>var x[i in AREAS] binary;</td>
</tr>
<tr>
<td>OBJECTIVE FUNCTION</td>
</tr>
<tr>
<td>maximise objective: sum [i in AREAS, j in EVALUATION CRITERIA] MULTI-CRITERIA EVALUATION MATRIX [i, j] * x[i];</td>
</tr>
<tr>
<td>CONSTRAINTS</td>
</tr>
<tr>
<td>s.t. (subject to) constraints_0: sum [i in AREAS] COST [i] * x[i] &lt;= BUDGET;</td>
</tr>
</tbody>
</table>

The \( n \) areas on which EIPs are realized (set AREAS) were evaluated according to \( k \) criteria (set EVALUATION CRITERIA), taking into account both morphological features of the place and the effects generated by the planned intervention.

The problem PARAMETERS were the:

- BUDGET,
- MULTI-CRITERIA EVALUATION MATRIX {AREAS, EVALUATION CRITERIA},
- COST {AREAS}.

The unknowns are binary, namely \( x \in \{0, 1\} \).

The objective function is:

\[
\text{maximize objective: sum [i in AREAS, j in EVALUATION CRITERIA] MULTI-CRITERIA EVALUATION MATRIX [i, j] * x[i]};
\]

The constraints system (CONSTRAINTS) are to do with the financial allocation available:

\[
\text{s.t. constraint_0: sum [i in AREAS] COST[i] * x[i] \leq \text{BUDGET}}.
\]

The CPLEX optimization program was used as a solver implementing the Brunch & Cut (B & C) algorithm to solve the Integer Linear Programming problems.
4. Results

Case Study

For application of the proposed model, eight areas to be redeveloped through regeneration initiatives, including urban forestry actions, were assumed.

Due to the limited budget available—the imagined equivalent of €1,000,000, which does not allow for the financing of all initiatives—the evaluation question expressed by the public administration sector was to select the areas able to generate the best financial, social, cultural, and environmental repercussions in the urban context within which they are proceeding, while using the available financial resources as best as possible.

Each area was evaluated according to following targets:

a. Improvement of the psycho-physical health of citizens,

b. Protection of the existing natural component,

c. Development of the environmental-economic context system,

all referable to the 14 criteria identified in Column C of Figure 2 used to express the degree of target achievement.

All 14 evaluation criteria and specific performance indicators were considered for case-study resolution.

For measurement of qualitative indicators, a values set {1, 3, 5} was used, which made it possible to attribute an increasing score to the \( i \)-th area on the basis of the ability to pursue the target through the intervention.

The values of the indicators are illustrated in the multi-criteria analysis matrix of Table 2. This table also shows the investment cost of each project.

<p>| Table 2. Multi-criteria analysis matrix. |</p>
<table>
<thead>
<tr>
<th>Area</th>
<th>Cost (Thousand of €)</th>
<th>Recreational Targets</th>
<th>Structure-Strengthening Targets</th>
<th>Ecological Targets</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>610</td>
<td>1.1 100</td>
<td>1.2 2 0 0 1 3</td>
<td>1.3 3 3 1 1 3 5 3 1 1 1</td>
</tr>
<tr>
<td>2</td>
<td>480</td>
<td>120 3 0 0 3 5 5 5 5 5</td>
<td>3 3 3 5 3 5 5 3 5 5 5 5 3 5 5 0 1</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>365</td>
<td>50 0 1 1 3 3 3 5 3 5 3 5 5 1 2 0 5</td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>200</td>
<td>95 0 0 1 1 3 3 5 3 5 3 5 5 1 1 0 3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>420</td>
<td>78 5 1 1 1 1 1 1 5 5 5 5 5 1 0 3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>300</td>
<td>150 2 0 0 3 1 3 3 5 1 3 3 3 3 1 1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>218</td>
<td>200 0 1 0 1 3 3 3 1 3 3 2 1 3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>122</td>
<td>0 1 1 0 1 5 1 1 3 1 5 5 0 5</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The model outlined in Section 3.2 was implemented with reference to data in Table 2. In the end, the .mod file of the analysis protocol was written such as in Table 3.

<p>| Table 3. The .mod file of the model. |
| --- | --- | --- | --- | --- | --- | --- | --- | --- |</p>
<table>
<thead>
<tr>
<th>Area</th>
<th>Cost (Thousand of €)</th>
<th>Recreational Targets</th>
<th>Structure-Strengthening Targets</th>
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</tr>
</thead>
<tbody>
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<td>1</td>
<td>610</td>
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<td>1.3 3 3 1 1 3 5 3 1 1 1</td>
</tr>
<tr>
<td>2</td>
<td>480</td>
<td>120 3 0 0 3 5 5 5 5 5</td>
<td>3 3 3 5 3 5 3 5 5 5 5 5 3 5 5 0 1</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>365</td>
<td>50 0 1 1 3 3 3 5 3 5 3 5 5 1 2 0 5</td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>200</td>
<td>95 0 0 1 1 3 3 5 3 5 3 5 5 1 1 0 3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>420</td>
<td>78 5 1 1 1 1 1 1 5 5 5 5 5 5 1 0 3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>300</td>
<td>150 2 0 0 3 1 3 3 5 1 3 3 3 3 1 1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>218</td>
<td>200 0 1 0 1 3 3 3 1 3 3 2 1 3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>122</td>
<td>0 1 1 0 1 5 1 1 3 1 5 5 0 5</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

## definition of areas ##

set AREAS (FORESTS);

set EVALUATION CRITERIA;

## parameters of the selection problem ##

param BUDGET;

param MULTI-CRITERIA EVALUATION MATRIX [AREAS (FORESTS), EVALUATION CRITERIA];

param COST [AREAS (FORESTS)];

## explication of the variable ##

var x[i] in AREAS (FORESTS) binary;

### objective function ###

maximize objective: sum{i in AREAS (FORESTS), j in EVALUATION CRITERIA} MULTI-CRITERIA EVALUATION MATRIX [i, j] × x[i];

### financial constraint ###

s.t. constraint_0: sum{i in AREAS (FORESTS)} COST[i] × x[i] ≤ BUDGET;
The .mod file in Table 3 associates with the .dat file in Table 4, which includes the multicriteria analysis data of Table 2.

Table 4. .dat file of the model written in AMPL.

```
set AREAS (FORESTS) := 1 2 3 4 5 6 7 8;
set EVALUATION CRITERIA := C1 C2 C3 C4 C5 C6 C7 C8 C9 C10 C11 C12 C13 C14;
param MULTI-CRITERIA EVALUATION MATRIX:
  C1  C2  C3  C4  C5  C6  C7  C8  C9  C10  C11  C12  C13  C14 :=
1  100  2  0  0  1  3  3  1  1  3  5  3  1  1
2  120  3  0  0  3  5  5  5  5  3  5  5  0  1
3  50  0  1  1  3  3  3  5  3  5  1  2  0  5
4  95  0  0  1  1  3  5  3  5  1  1  1  0  3
5  78  5  1  1  1  1  1  5  5  5  1  0  3
6  150  2  0  0  3  1  3  5  1  3  3  3  1  1
7  200  0  1  0  1  3  3  3  1  3  3  2  1  3
8  0  1  1  0  1  5  1  1  3  1  5  5  0  5;
```

```
param BUDGET := 1000;
param COST :=
  1  610
  2  480
  3  365
  4  200
  5  420
  6  300
  7  218
  8  122;
```

The .mod and .dat files are named within the AMPL command line (Table 5) in which the solver that implements the Branch & Cut algorithm is specified.

Table 5. Command lines in AMPL.

```
ampl: reset;
ampl: model.mod FILE;
ampl: data.dat FILE;
ampl: option solver cplex;
ampl: solve.
```

Table 5 shows the results. The optimal combination is obtained with areas 2, 6, and 7, whose urban forestry interventions make it possible to maximize the effects of the different nature that can be generated in the surrounding context and use the available financing in the best way possible, minimizing the unused portion of it that returns to the financial institution.

Table 6. Command lines in AMPL.

```
ampl: display x;
x [*] :=
  1  2  3  4  5  6  7  8
0  1  0  0  0  1  1  0;
```

```
ampl: objective function := 560
```

5. Conclusions

A systemic vision between the natural and built environment suggests using alternative action strategies, with respect to those ordinarily pursued, in the redevelopment of degraded urban areas, addressing them in the context of the sustainable development of a city that harmoniously contemplates various financial, social, cultural, and environmental aspects. In this sense, interventions that include
urban forestry actions are able to generate ecosystemic effects that can support the existing vegetation protection, economic growth of the territory, and the psycho-physical wellbeing of the citizens.

In cases where it is necessary to establish which—among those available—are the city portions to be redeveloped according to ecosystemic logics, it is important to have decision support tools that allow to identify the optimal allocation of the available financial resources in the functions of returns and eco-system services generated. According to the multidimensional nature of these initiatives, it is necessary to use the tools available to consider the complexity of the effects produced, obviously respecting the intrinsic characteristics of the area to be recovered.

In this work, an innovative multi-criteria model of Linear Discrete Programming was proposed and tested in order to define the optimal combination of interventions to be financed for sustainable urban development. The model can support the public administration sector in the planning of urban interventions defined according to integrated ecosystemic principles. For particularly complex cases characterized by numerous constraints and many variables, the model makes it possible to select the most suitable areas for urban forestry initiatives, as it is able to maximize the effects on the collective.

In order to express the various ecosystemic services generated by forestry actions, each intervention alternative is evaluated according to appropriate performance indicators. The use of multiple indicators makes it possible to select the best design solution based not only on financial parameters, but also social, cultural, and environmental ones. The result is the construction of an investment program defined in an effective and transparent manner, in line with the objectives of urban recovery and the enhancement of a natural and built environment.

The evaluation protocol, written with “A Mathematical Programming Language” in the .mod file, has input data derived from multicriteria analysis included in the .dat file. These data are then implemented through the B&C Optimization Algorithm, which resolves the optimization model composed of an objective function and which is subject to constraint conditions. The algorithm provides the best combination of the areas to be redeveloped through EIPs.

On the basis of the results obtained with the implementation of the proposed model, the set of areas (2, 6, 7) returns the highest value of the objective function (560), and the sum of the corresponding investment costs (€998,000.00) responds to the constraint about the available budget (€1,000,000.00).

Among the positive aspects of the model, the flexibility which derives from the nature of operational research, and thanks to which the mathematical relationships that translate the objectives and model constraints can be easily adapted to any changes in the technical, political, and economic context that could happen over time, should certainly be stressed.

In this sense, interesting research perspectives hold the possibility of modifying the model parameters to different urban realities, as well as the verifications relating to the concrete applicability of the model.

Author Contributions: A.N., M.R.G., P.M., F.S. have conceived, structured and written the article in equal part, as well as they have deepened review and editing the proposed article. In particular, A.N. and F.S. have implemented the software; M.R.G. and P.M. have validated the calculations; A.N. and M.R.G. have made work supervision.

Funding: This research received no external funding.

Conflicts of Interest: The authors declare no conflict of interest.

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